

# The Structural Richness of Beliefs About Norms: Challenges for Empirical Elicitation

Glenn Harrison and Don Ross



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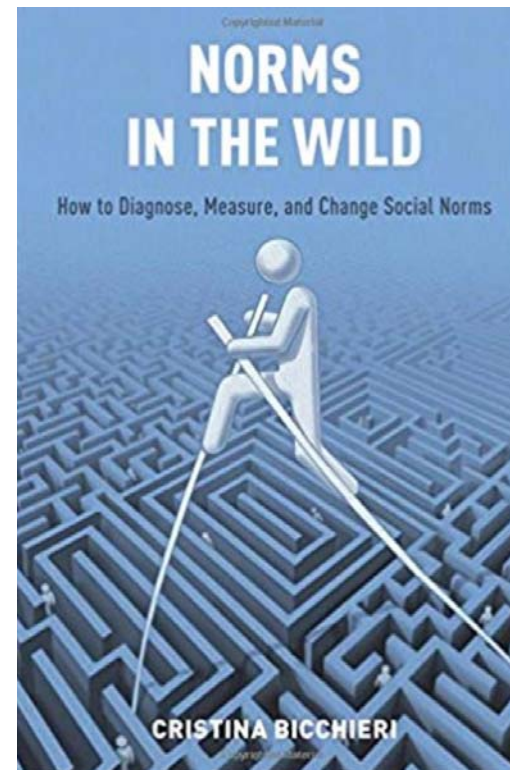
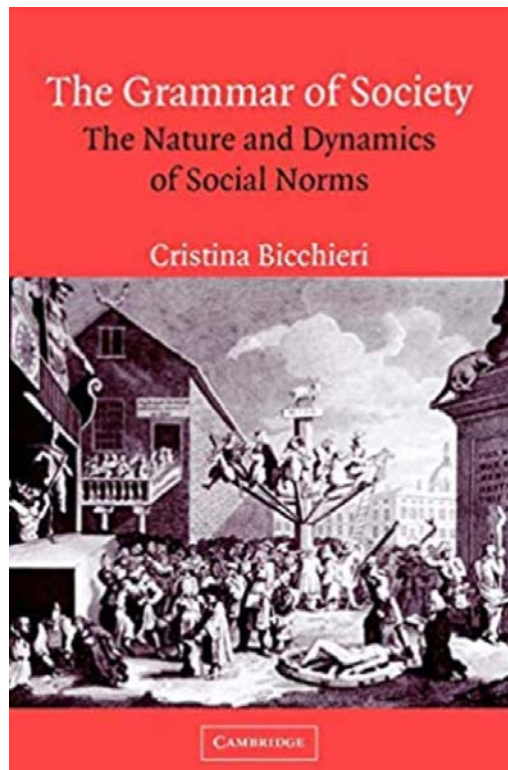
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# Outline

- Defining norms in terms of belief consistency
- Problems arise with leading experimental tests
  - Belief distributions  $\neq$  mean or mode
  - No discussion of confidence of beliefs
  - No discussion of statistical consistency of beliefs
- Elements of an improved experimental approach
- New theoretical approach for games with norms



# Defining norms



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# Defining norms

- Descriptive beliefs
  - First-order: what does an agent believe others will do?
  - Second-order: what does an agent believe others believe that others will do?
- Normative beliefs
  - First-order: what does an agent believe she and others should do?
  - Second-order: what does an agent believe others believe she and others should do?
- Conditional preference for following the norm
  - The conditionals are all four beliefs are consistent



# Defining norms

- Some subtleties
  - “in the appropriate circumstances”
  - “for the relevant group of people”
- Distinctions
  - “Social preference”: choosing as if abstract social states are arguments in the agent’s utility function
  - Conditional preference for following a social norm  $\neq$  a “social preference”



# Confidence in beliefs

- **Overestimation** of one's actual ability
- **Overplacement** of one's self relative to others
- **Overprecision**: excessive certainty about accuracy of one's beliefs



## The Trouble With Overconfidence

Don A. Moore  
Carnegie Mellon University

Paul J. Healy  
The Ohio State University

Psychological Review  
2008, Vol. 115, No. 2, 502–517



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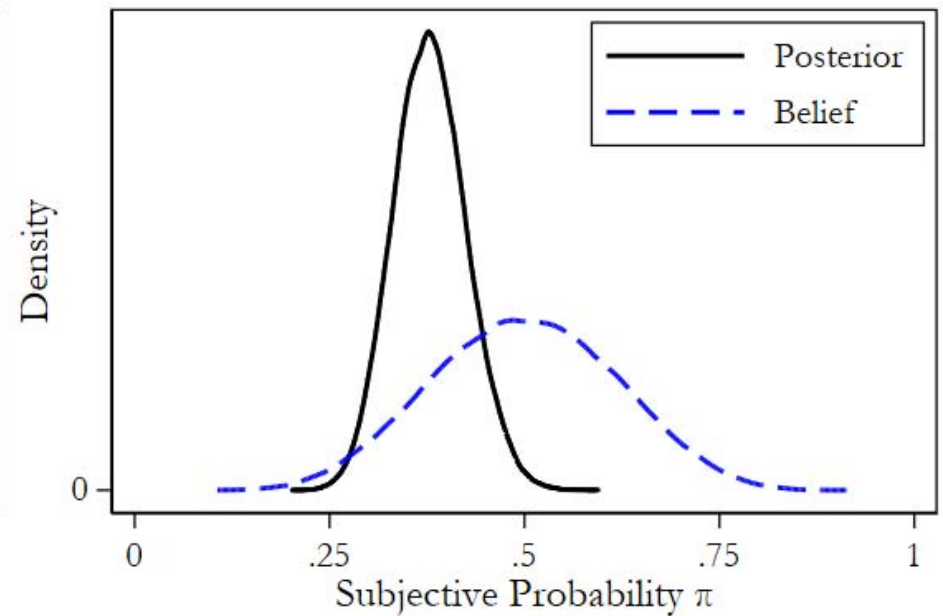
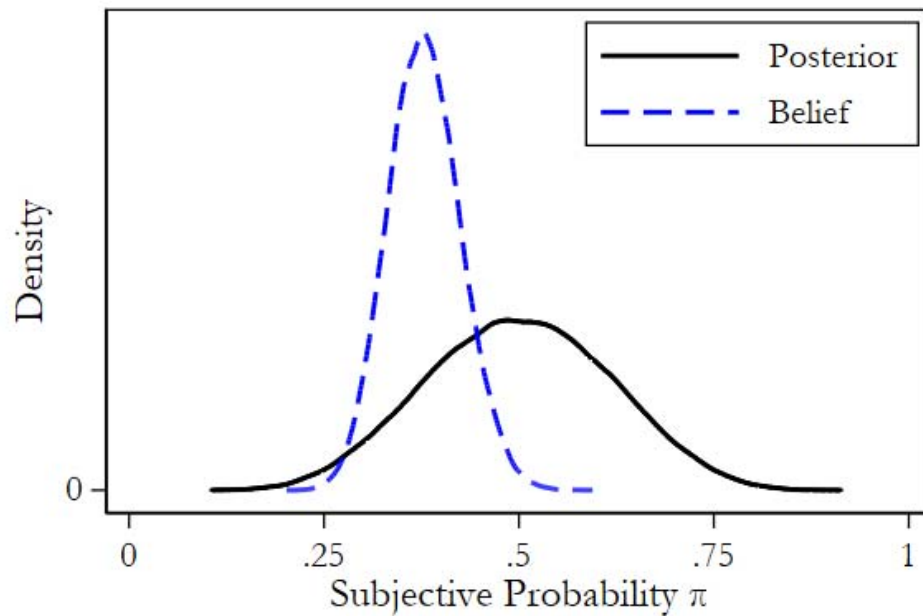
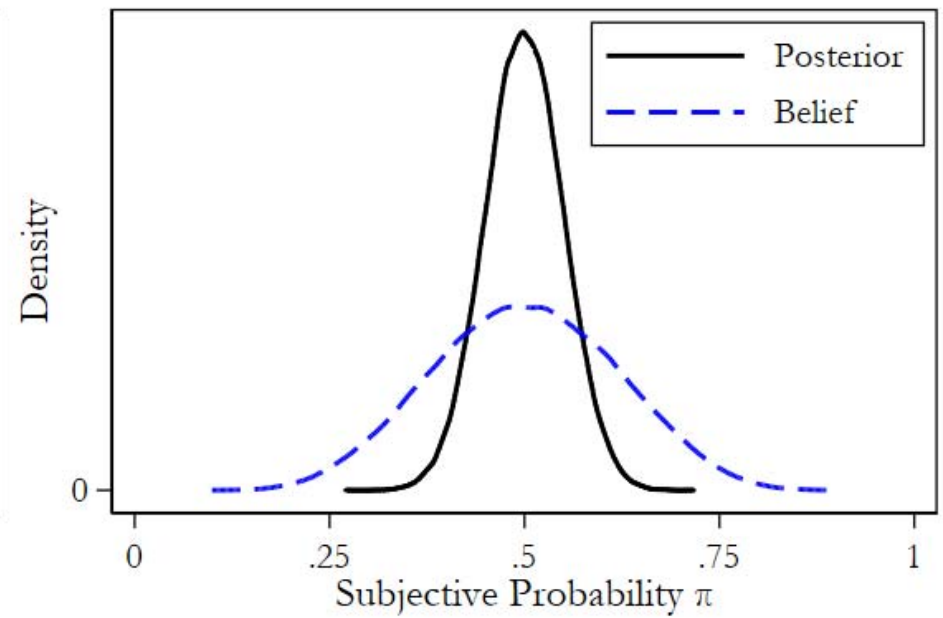
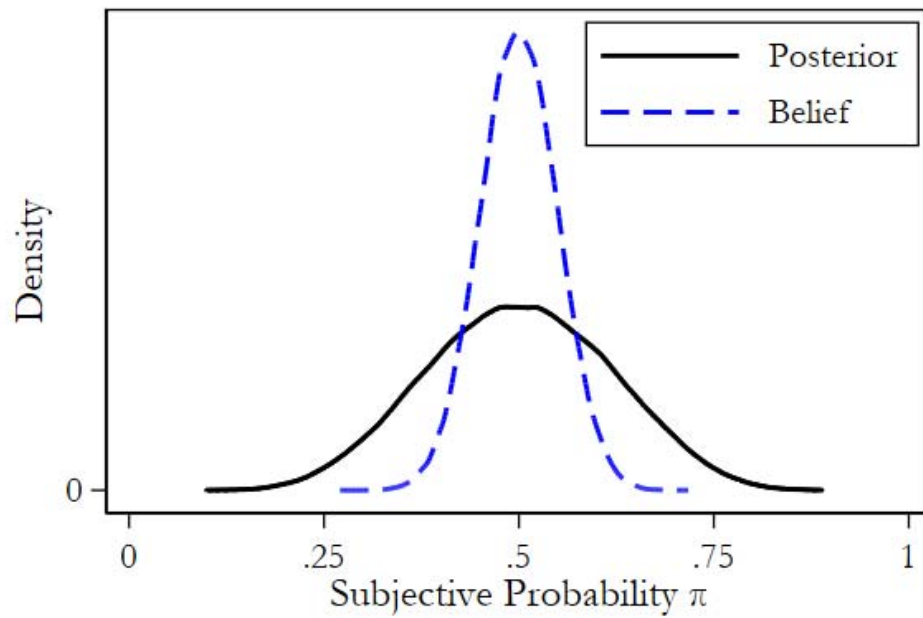


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# Bias and Confidence





# Eliciting subjective beliefs

- Use Quadratic Scoring Rules to incentivize
  - Risk preferences and beliefs jointly estimated
- Underlying events
  - Binary → subjective probability
  - Continuous → subjective probability density function
  - Categorical → subjective probability mass function
- Set aside debates over elicitation methods for now



# Our Team: CEAR and CEAR-Africa



Andre Hofmeyr



Brian Monroe



Dawn Wang



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## Estimating subjective probabilities

Steffen Andersen • John Fountain •  
Glenn W. Harrison • E. Elisabet Rutström



JOURNAL OF FINANCIAL AND QUANTITATIVE ANALYSIS Vol. 52, No. 2, Apr. 2017, pp. 737–750  
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doi:10.1017/S0022109017000035

## Information Characteristics and Errors in Expectations: Experimental Evidence

Constantinos Antoniou, Glenn W. Harrison, Morten I. Lau, and Daniel Read\*



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## Journal of Economic Behavior & Organization

journal homepage: [www.elsevier.com/locate/jebo](http://www.elsevier.com/locate/jebo)



### Scoring rules for subjective probability distributions<sup>☆</sup>



Glenn W. Harrison<sup>a,\*</sup>, Jimmy Martínez-Correa<sup>b</sup>, J. Todd Swarthout<sup>c</sup>,  
Eric R. Ulm<sup>d</sup>



# 7

## Subjective Beliefs and Statistical Forecasts of Financial Risks: The Chief Risk Officer Project

*Glenn W. Harrison and Richard D. Phillips*

2014



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# An Example: a Trust Game

- Player 1 and Player 2 each have \$100
- Player 1 can send \$0, \$20, \$40, \$60, \$80 or \$100
- Player 3, the experimenter, scales up by 3



# Beliefs about Player 1 choices

How much of the \$100 will Player 1 send to Player 2?



11 tokens  
pay \$26.03

20 tokens  
pay \$30.53

24 tokens  
pay \$32.53

18 tokens  
pay \$29.53

12 tokens  
pay \$26.53

15 tokens  
pay \$28.03



Unallocated tokens: 0

Submit

Submit your decision or  
continue making choices



# An Example: a Trust Game

- Player 1 and Player 2 each have \$100
- Player 1 can send \$0, \$20, \$40, \$60, \$80 or \$100
- Player 3, the experimenter, scales up by 3
- So Player 2 has \$0, \$60, \$120, \$240 or \$300 to send back to Player 1
- Strategy method used for choices
- Focus on beliefs about Player 2 choices if has \$60
  - Using data on choices from trust games run by CEAR-Africa



# First-order descriptive beliefs

How much of the \$60 received by Player 2 **will** be returned to Player 1?



5 tokens  
pay \$13.86

23 tokens  
pay \$22.86

70 tokens  
pay \$46.36

2 tokens  
pay \$12.36



Unallocated tokens: 0

Submit

Submit your decision or  
continue making choices



# First-order normative beliefs

How much of the \$60 received by Player 2 do **you** think **should** be returned to Player 1? **This is a hypothetical question**



5 tokens  
pay \$13.86

23 tokens  
pay \$22.86

70 tokens  
pay \$46.36

2 tokens  
pay \$12.36



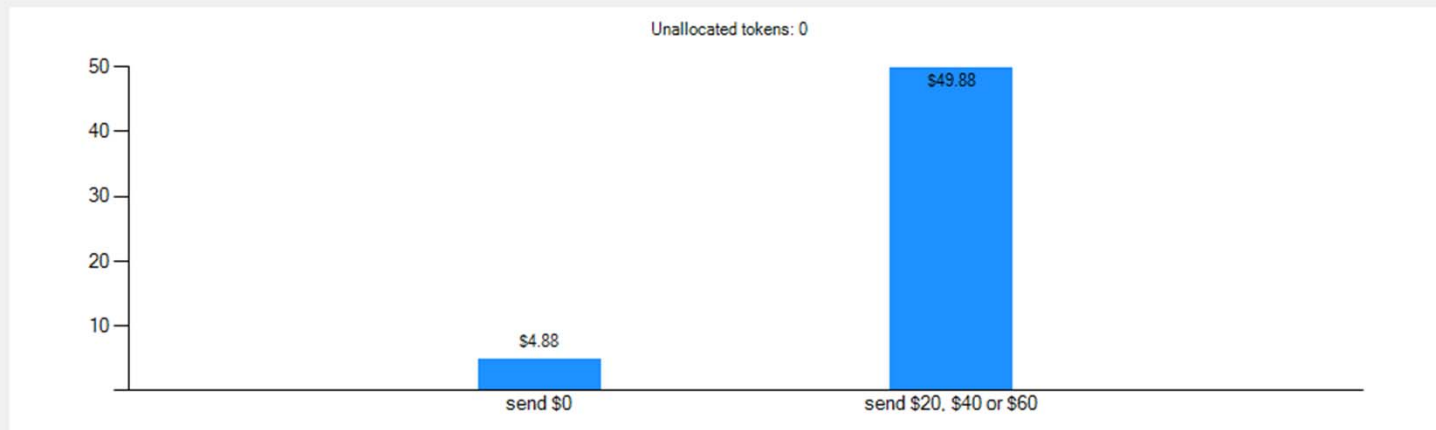
Unallocated tokens: 0

Submit

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# Second-order descriptive beliefs

If \$60 is sent to Player 2, what fraction of tokens will be allocated to **believing** that **\$0 will be sent back** to Player 1?



5 tokens  
pay \$4.88



95 tokens  
pay \$49.88



Unallocated tokens: 0

Submit

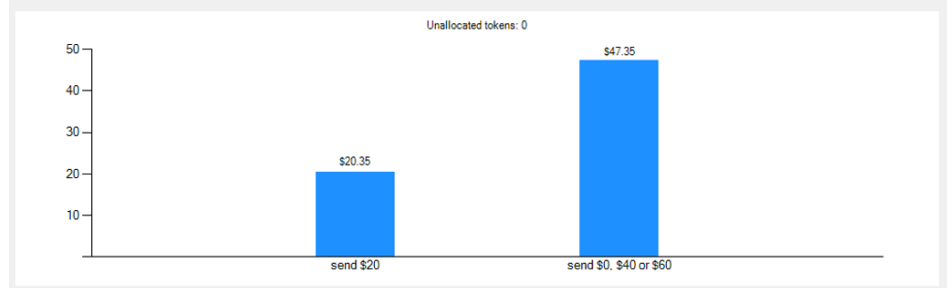
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# Second-order descriptive beliefs

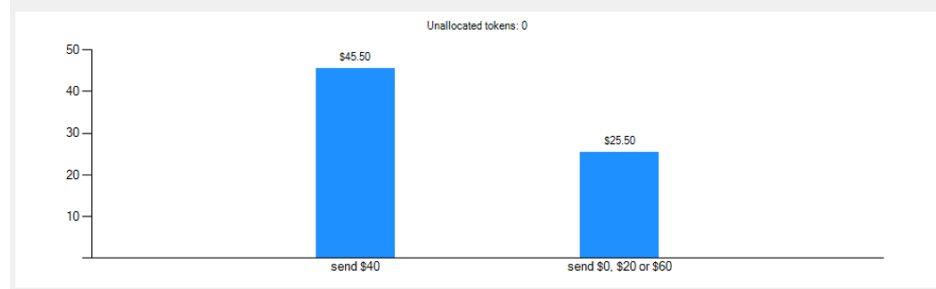
If \$60 is sent to Player 2, what fraction of tokens will be allocated to **believing** that **\$0 will be sent back** to Player 1?



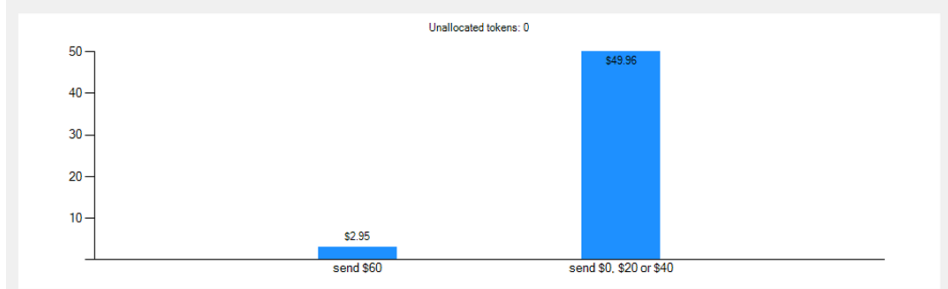
If \$60 is sent to Player 2, what fraction of tokens will be allocated to **believing** that **\$20 will be sent back** to Player 1?



If \$60 is sent to Player 2, what fraction of tokens will be allocated to **believing** that **\$40 will be sent back** to Player 1?

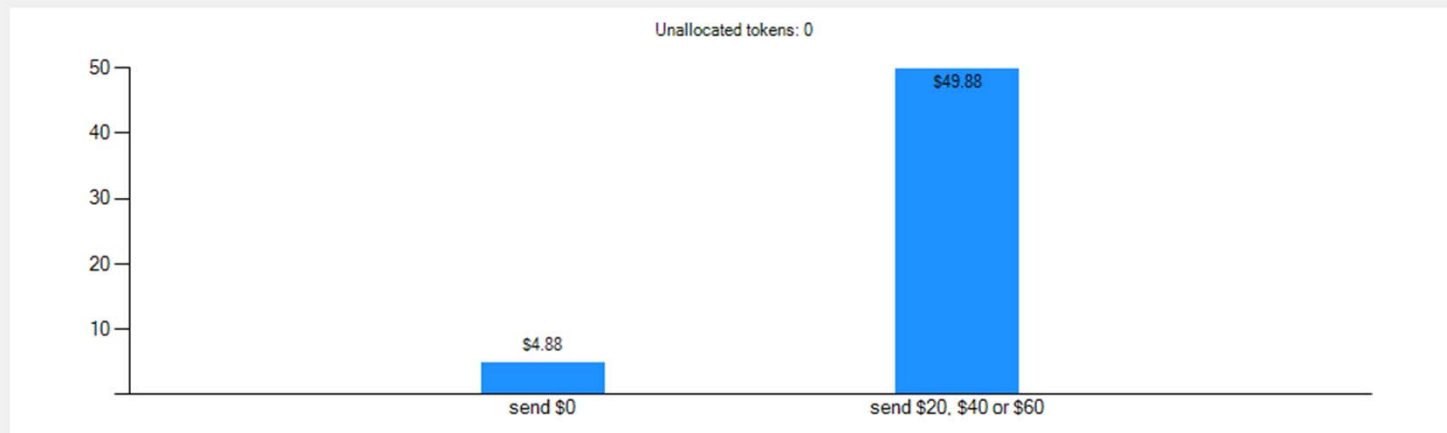


If \$60 is sent to Player 2, what fraction of tokens will be allocated to **believing** that **\$60 will be sent back** to Player 1?



# Second-order normative beliefs

If \$60 is sent to Player 2, what fraction of tokens will be allocated to **believing** that **she should** send back \$0 to Player 1?



5 tokens  
pay \$4.88



95 tokens  
pay \$49.88



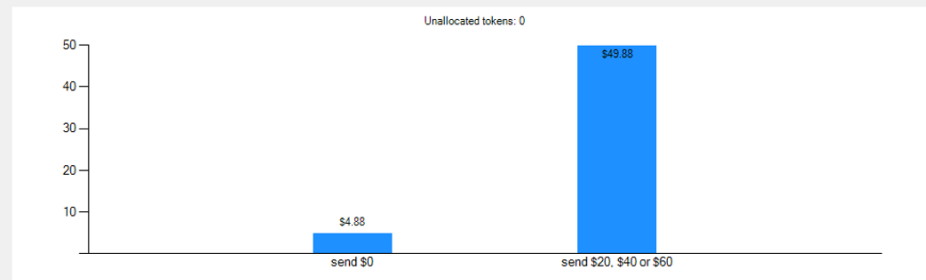
Unallocated tokens: 0

Submit

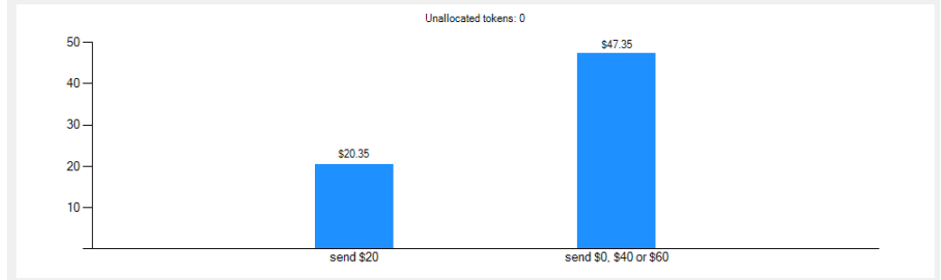
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# Second-order normative beliefs

If \$60 is sent to Player 2, what fraction of tokens will be allocated to **believing** that **she should** send back \$0 to Player 1?



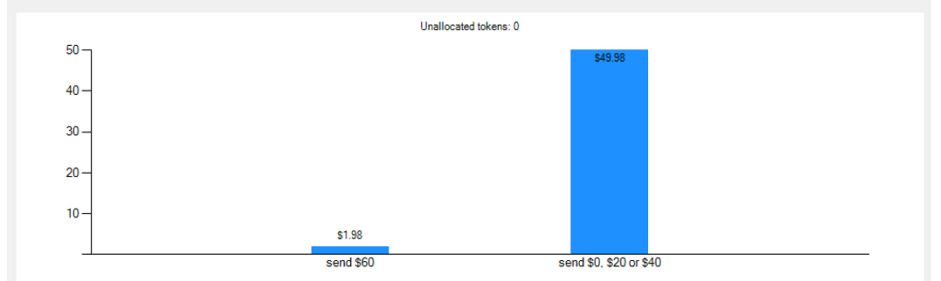
If \$60 is sent to Player 2, what fraction of tokens will be allocated to **believing** that **she should** send back \$20 to Player 1?



If \$60 is sent to Player 2, what fraction of tokens will be allocated to **believing** that **she should** send back \$30 to Player 1?



If \$60 is sent to Player 2, what fraction of tokens will be allocated to **believing** that **she should** send back \$60 to Player 1?



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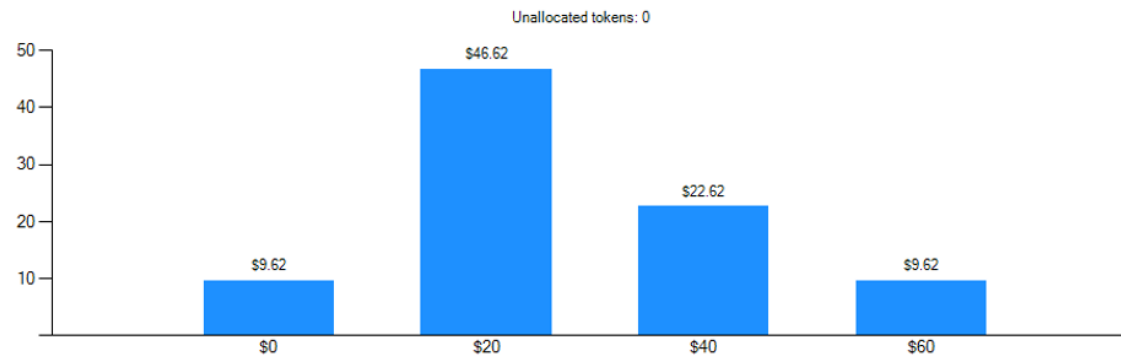
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# Belief inconsistency, $1D \neq 1N$

How much of the \$60 received by Player 2 **will** be returned to Player 1?



How much of the \$60 received by Player 2 do **you** think **should** be returned to Player 1? **This is a hypothetical question**



# Belief inconsistency, $1D \neq 1N$

How much of the \$60 received by Player 2 **will** be returned to Player 1?



How much of the \$60 received by Player 2 **do you think should** be returned to Player 1? **This is a hypothetical question**



# Belief inconsistency, $1D \neq 2N$

How much of the \$60 received by Player 2 **will** be returned to Player 1?



If \$60 is sent to Player 2, what fraction of tokens will be allocated to **believing** that **she should** send back \$20 to Player 1?





# Evaluating consistency

- Now a simple statistical problem
- Not the same as a distribution of point estimates from a sample
  - Often confused with uncertainty of beliefs
  - Many examples: inflation expectations



# Evaluating consistency

- Now a simple statistical problem
- Not the same as a distribution of point estimates from a sample
  - Often confused with uncertainty of beliefs
  - Many examples: inflation expectations
- Statistical tests for consistency w.r.t. bias
- Statistical tests for consistency w.r.t. confidence
- Statistical tests for consistency of **both**



# Statistical insights

- Consistency measured by more than just bias
- Statistical measures of degree of consistency
  - Overall consistency:  $1D = 1N = 2D = 2N$
  - Partial consistency:  $1D = 1N$ ,  $1D = 2D$  or  $1N = 2N$
- Identification of degree of consistency of different “reference networks” by demographics
- Identification of influential “norm disruptors”
- Identification of those with “norm wiggle room”



# What is done in the literature?

- No incentives on elicitation of normative beliefs
  - Incentives  $\neq$  incentive-compatibility
- Assume risk neutrality
- Elicit a subjective probability of a binary event
  - No role for confidence at all
- Elicit a statistic of a belief distribution
  - Mode: “tell me your belief and I’ll pay you \$x if you are correct”



# What we will do

- Trust games (incentives)
- Risk preference elicitation (incentives)
- Elicit first-order descriptive beliefs (incentives)
- Survey first-order normative beliefs (no incentives)
- Elicit second-order normative beliefs (incentives)
- Do subjects in a second trust game pay a premium to play with others based on information about first-order normative beliefs?

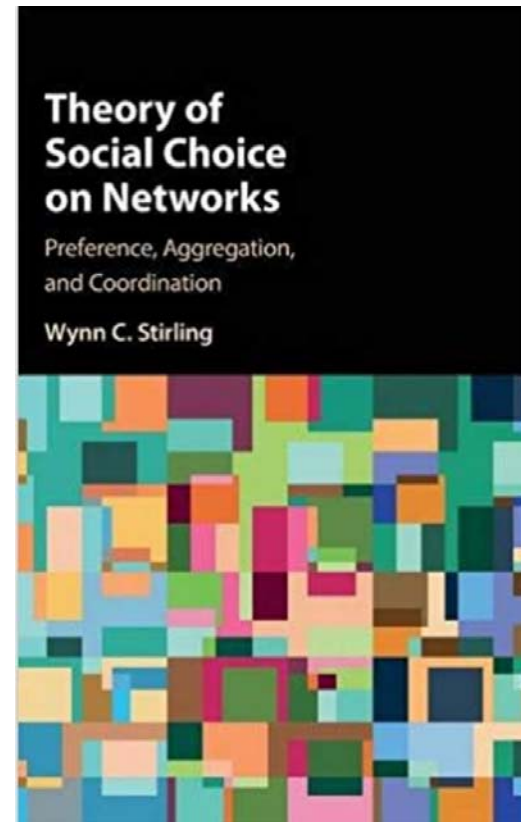
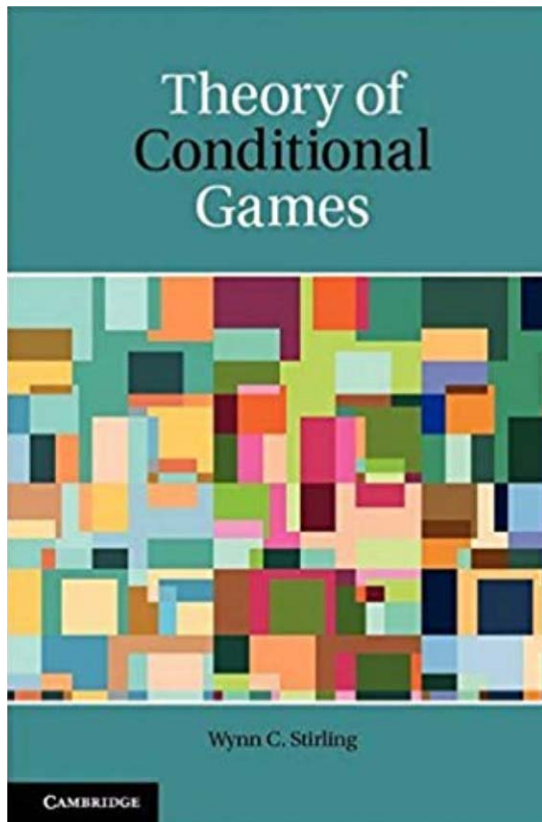


# Analyzing trust game play

- Unconditional Nash Equilibrium
- Unconditional Quantal Response Equilibrium
- Conditional Nash Equilibrium
- Conditional Quantal Response Equilibrium



# Theory of Conditional Games



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# Conditional Game Theory

- Distinguish *categorical* & *conditional* preferences

Categorical preferences *unconditionally* define an agent's ranking of possible outcomes, regardless of other agents' preferences

Conditional preferences are based on influence flows which propagate through a group and define agents' rankings of alternative outcomes as *conditional* on the preferences of others

Model this propagation of influence flows by applying the formal syntax of probability theory to game theory, and constructing a representation with Bayesian belief networks





# Probability syntax & normative uncertainty

The conventional application of the probability syntax is as a means of expressing epistemological uncertainty regarding belief

This logical structure may be used in expressing behavioral uncertainty regarding preference: just as agent  $i$  is ***epistemologically*** uncertain if  $i$  does not have complete knowledge that a proposition is realized, so  $i$  is ***normatively*** uncertain if  $i$  is not completely decisive that an action should be taken



# Norms for norm research

- Beliefs about what norms are
- Beliefs about how to elicit beliefs
- Beliefs about how to measure consistency
  - Critical statistical role for confidence here
  - Insights about heterogeneity of “reference networks”
- Beliefs about the formal conditionality of preferences in contexts where norms apply

